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ASIAN INSTITUTE OF TECHNOLOGY

# Mobile Robot Path Planning and Navigation Control

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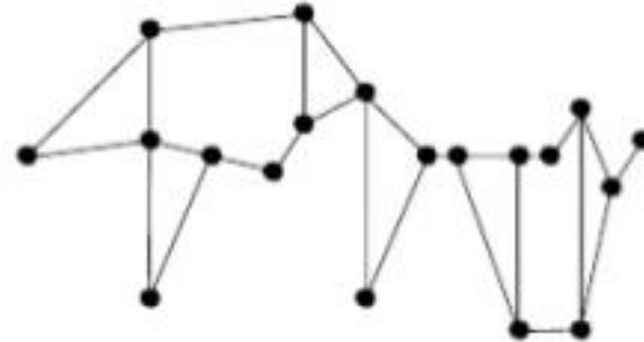
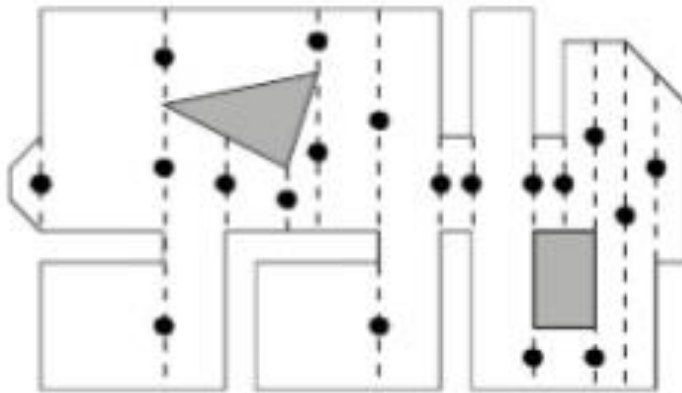
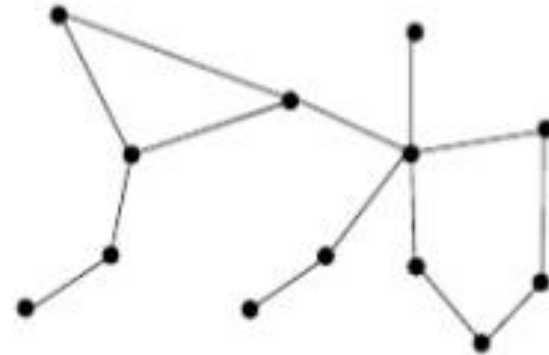
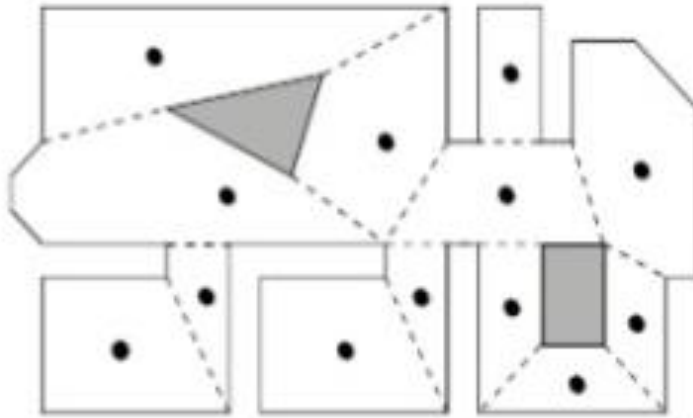
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# Mobile Robot Path Planning

- Global Path Planning (Off Line)
  - Cell Decomposition
  - Road Map
  - Visibility Graph
  - Optimized by A-Star, PSO, GA, etc.
- Local Path Planning (On Line)
  - Potential Field
  - Virtual Forces
  - Rule Based
  - Behavior Based
  - Model Based (PID, State-Space, etc.)

# Global Path Planning

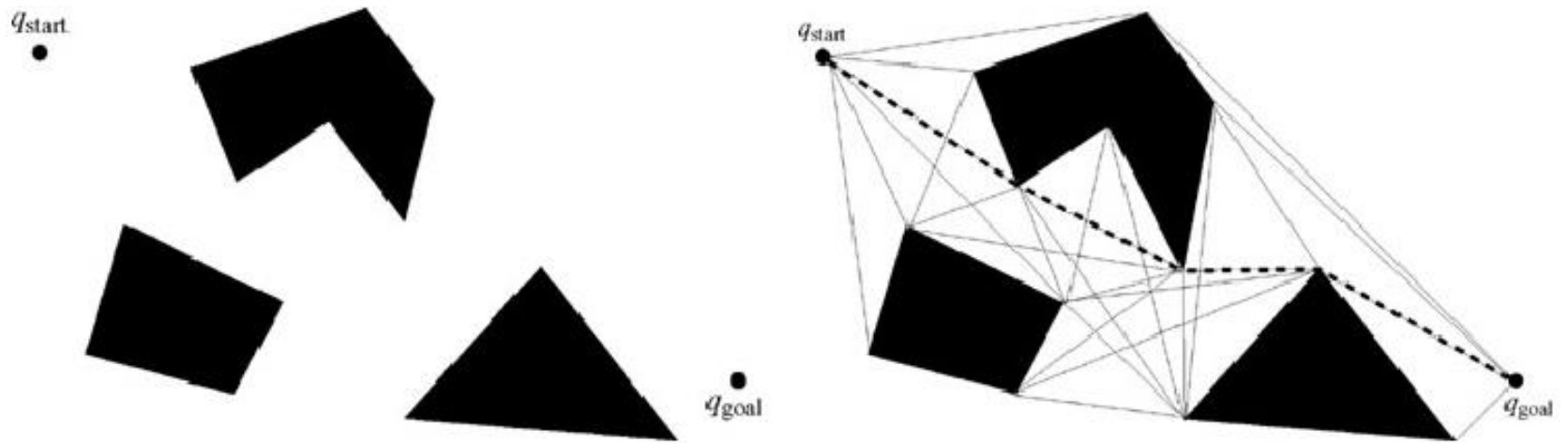
# Cell Decomposition



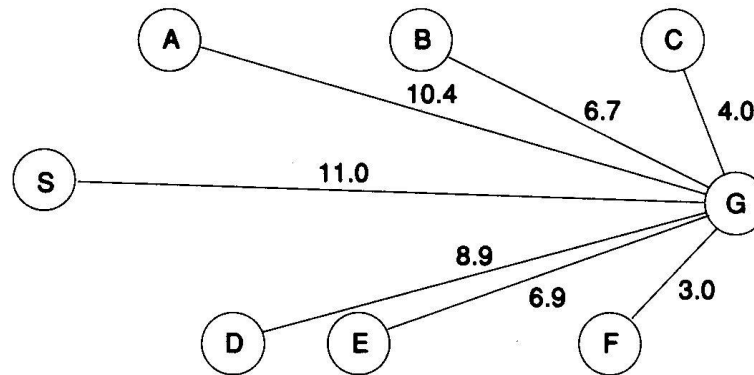
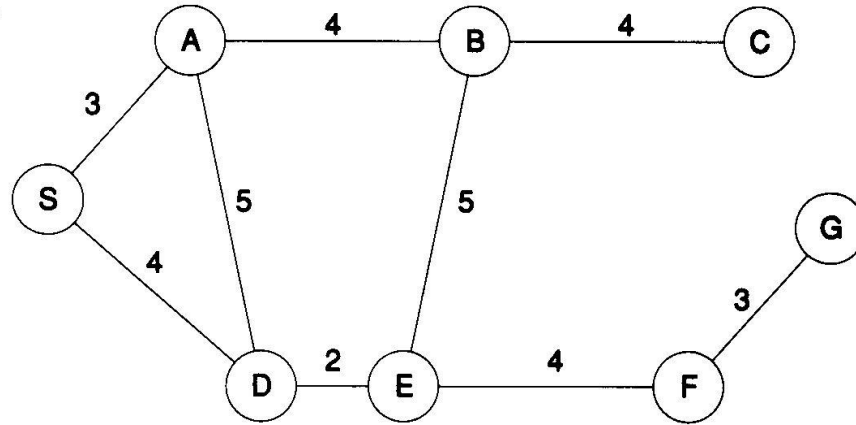
# Road Map



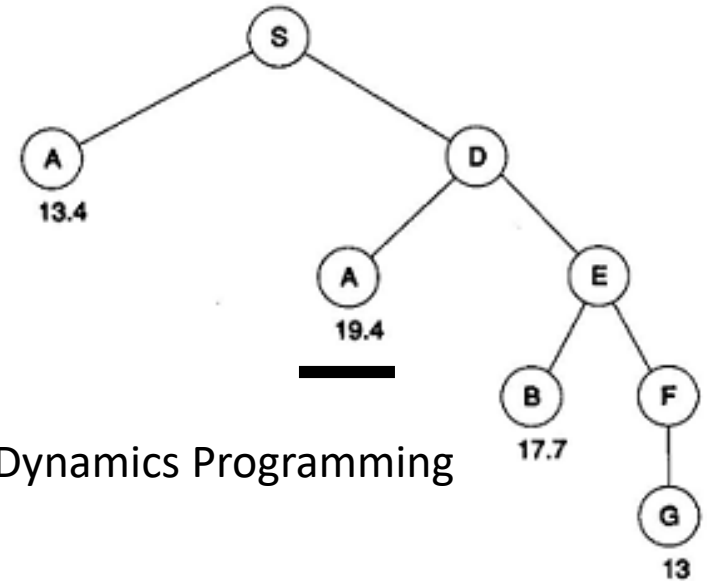
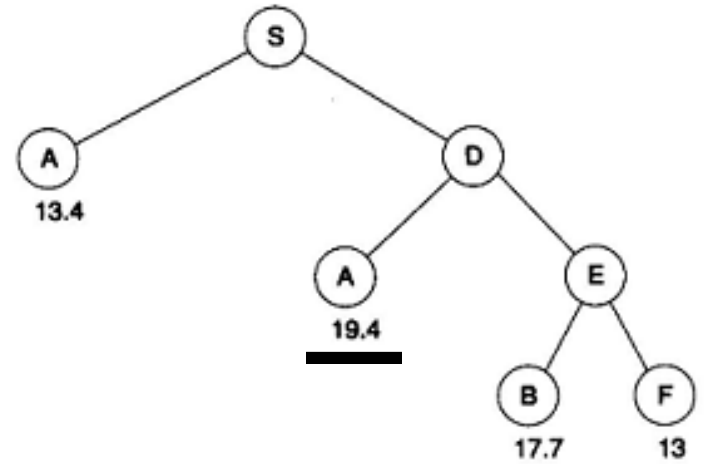
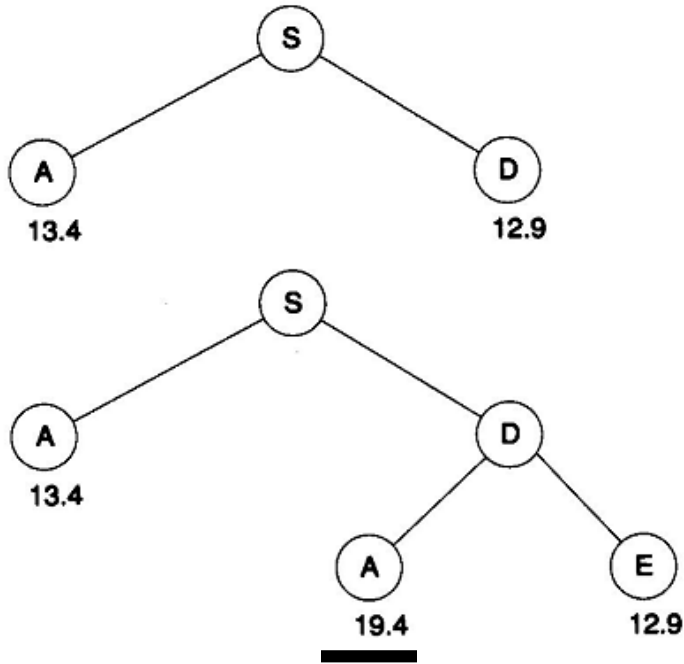
# Visibility Graph



# Optimal Search



# A-Star

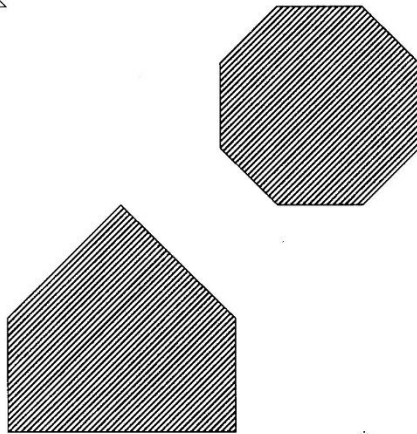
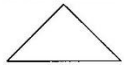


A-Star = Branch and Bound + Under Estimation + Dynamics Programming



# A-Star in Path Planning

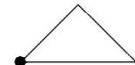
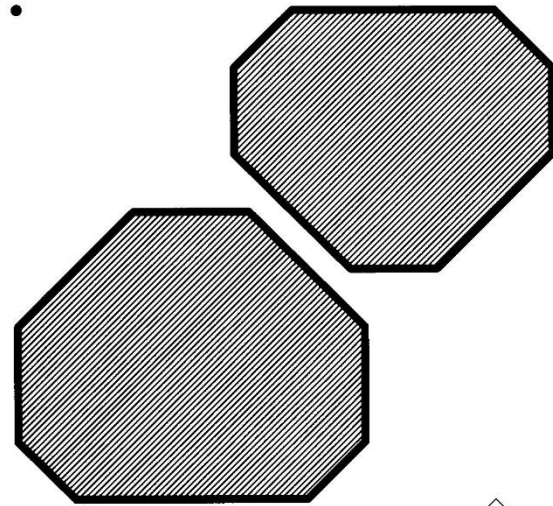
Initial position



Desired position



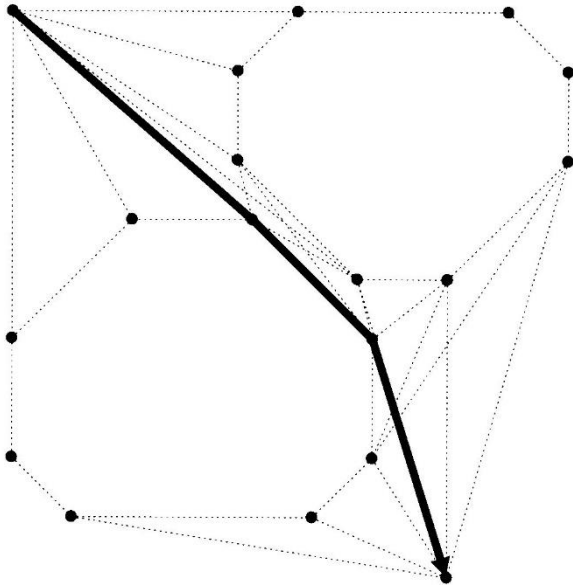
Initial position



Desired position

# A-Star in Path Planning

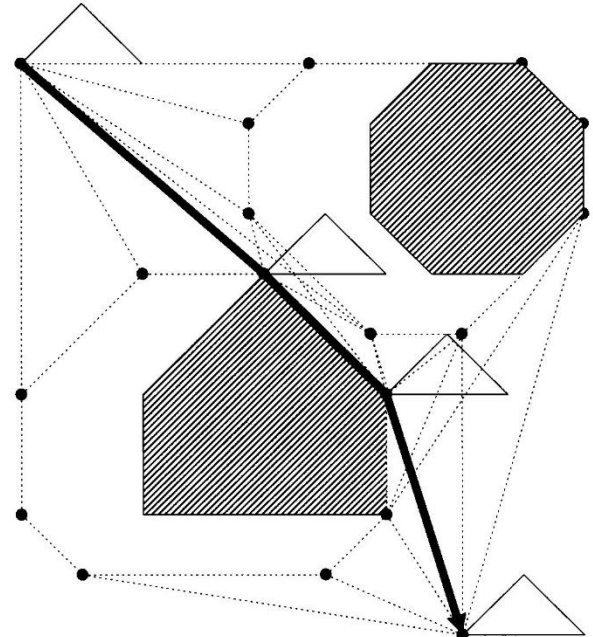
Initial position



Desired position

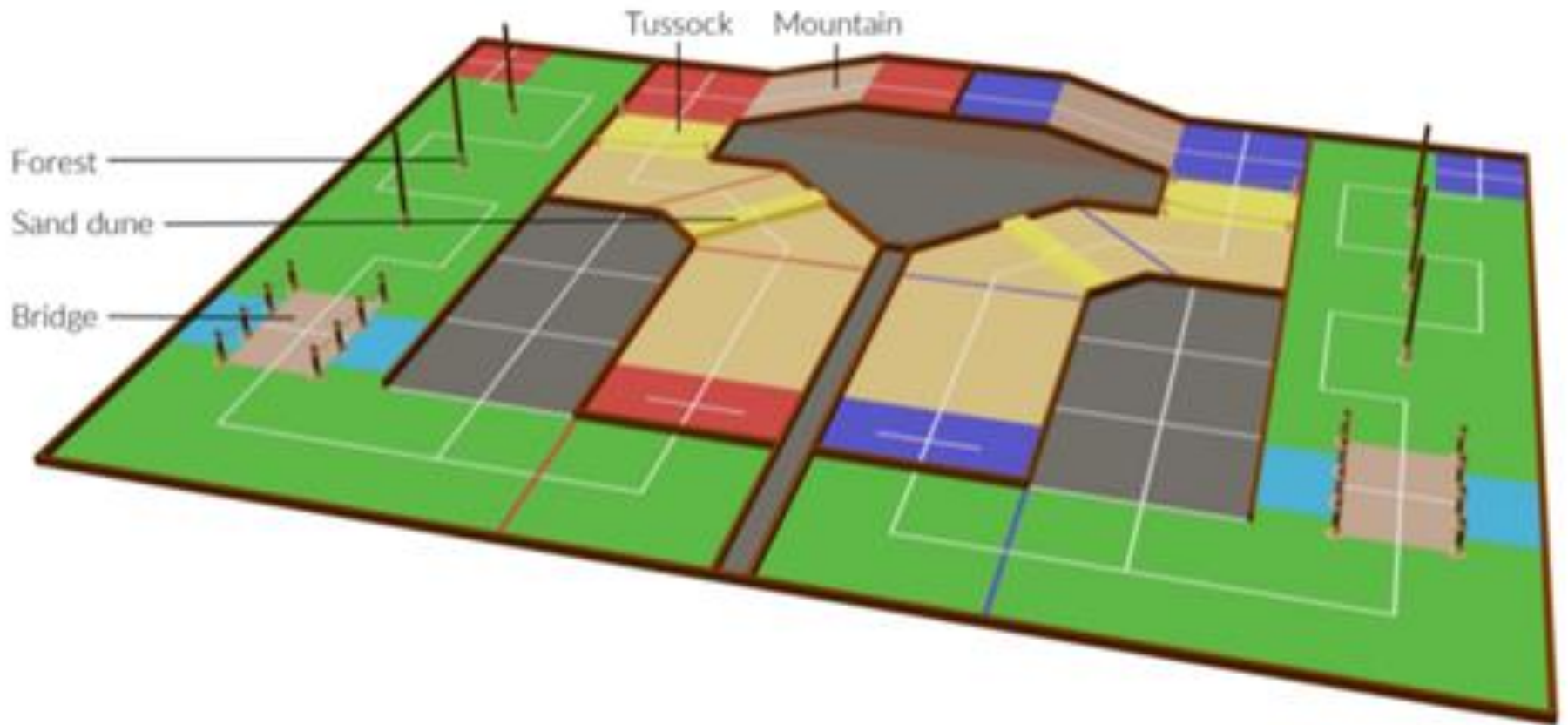


Initial position



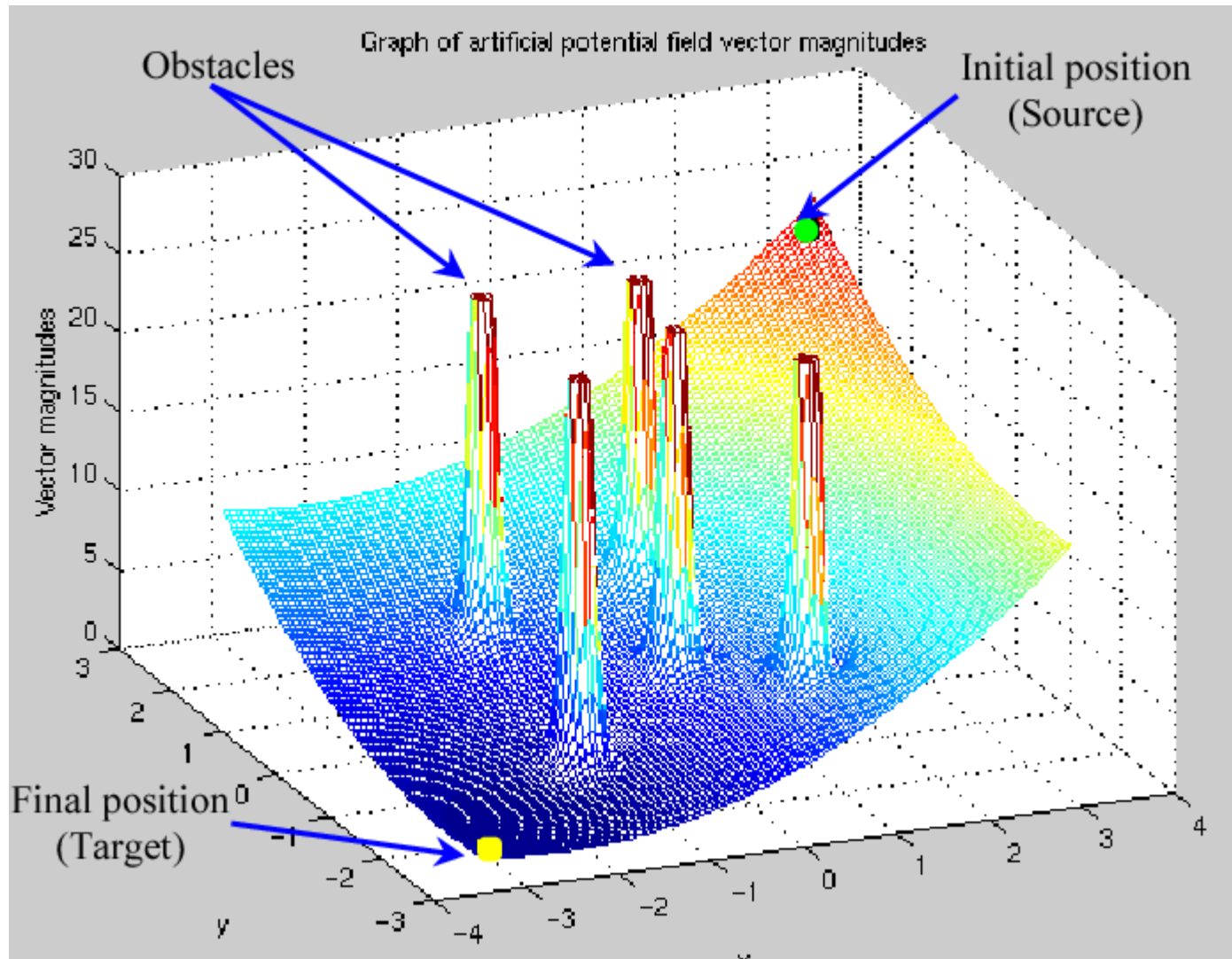
Desired position

# Global Path Planning of ABU Robocon 2019

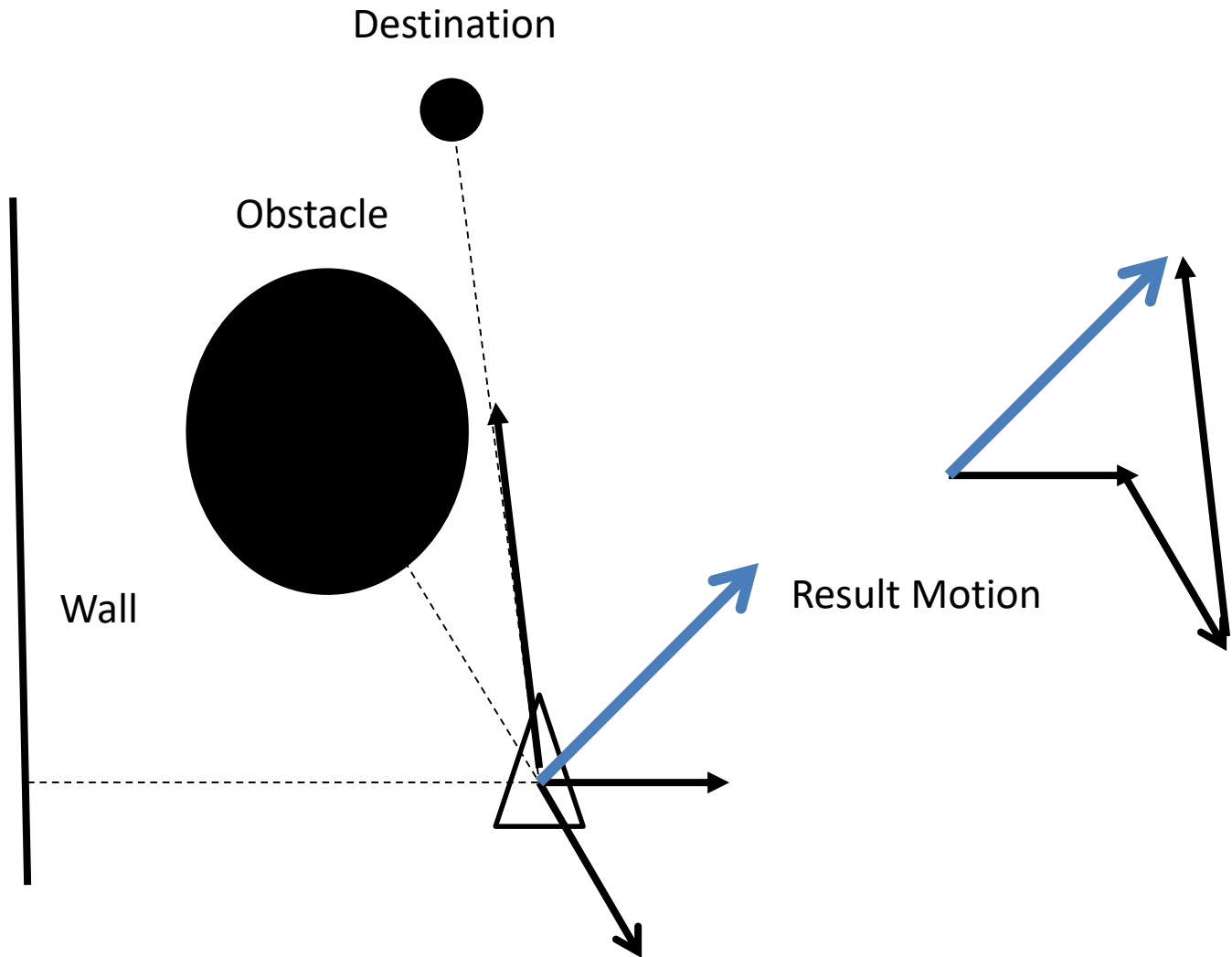


# Local Path Planning

# Potential Field



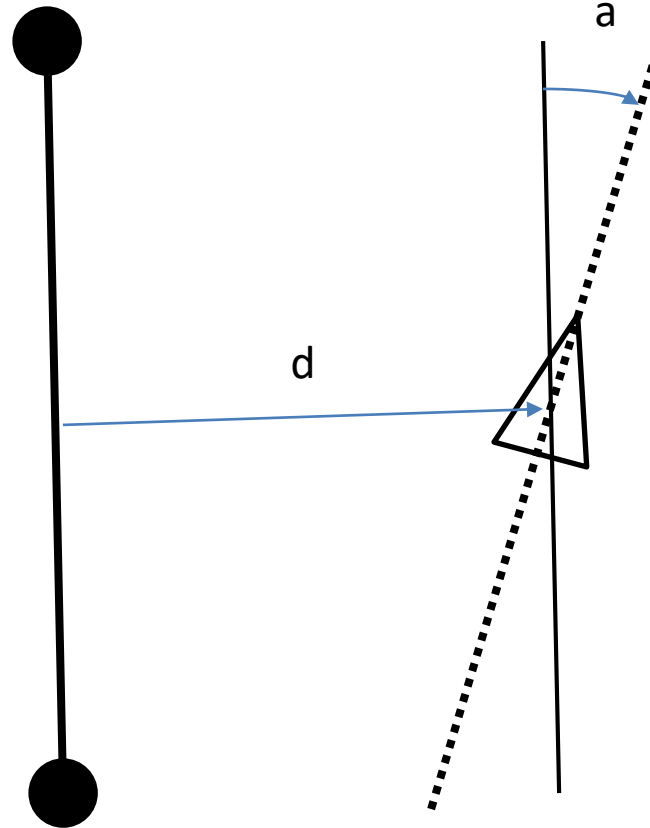
# Virtual Forces



$$\text{Virtual Force} = \text{Virtual Spring Force} + \text{Virtual Damping Force}$$

# Waypoint Tracking (Road)

Next Waypoint

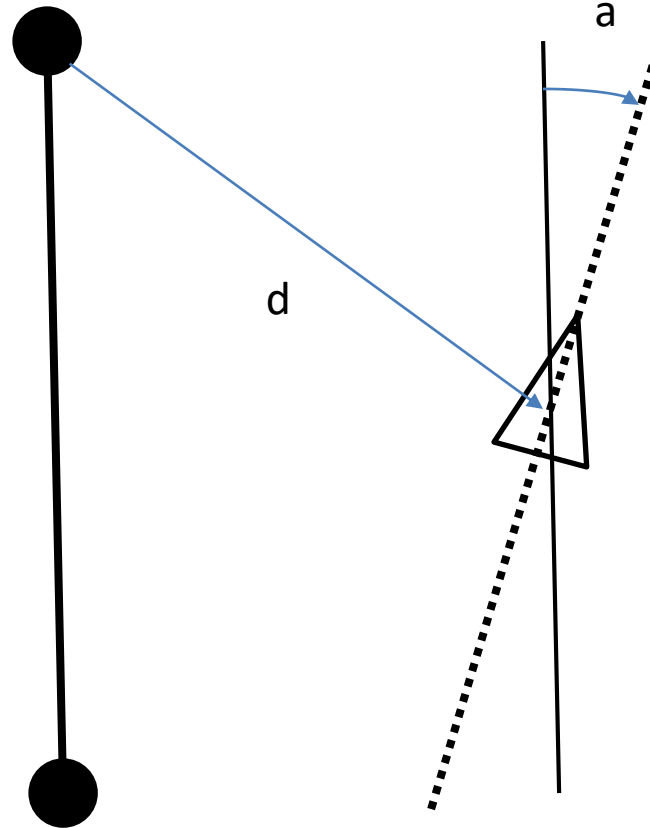


Previous Waypoint

$$\textit{Steering} = K_{dis\_P}(d) + K_{dis\_D}(\dot{d}) + K_{head\_P}(a) + K_{head\_d}(\dot{a})$$

# Waypoint Tracking (Field)

Next Waypoint



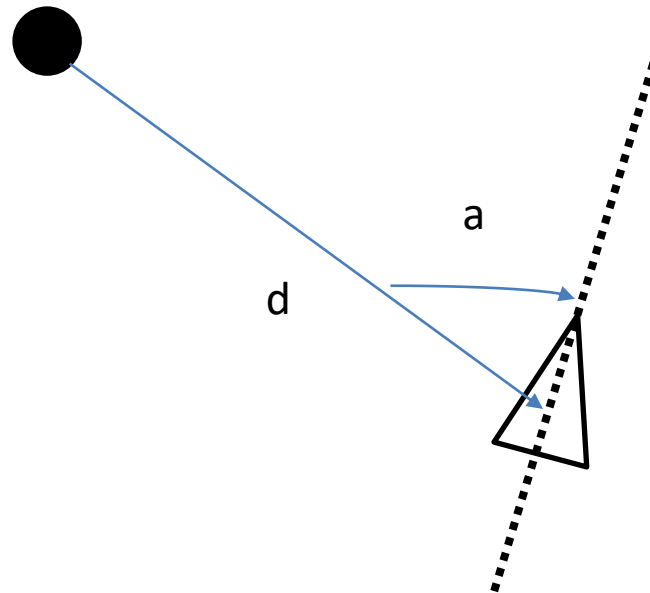
Previous Waypoint

$$\textit{Steering} = K_{dis\_P}(d) + K_{dis\_D}(\dot{d}) + K_{head\_P}(a) + K_{head\_d}(\dot{a})$$



# Waypoint Tracking (Field)

Next Waypoint

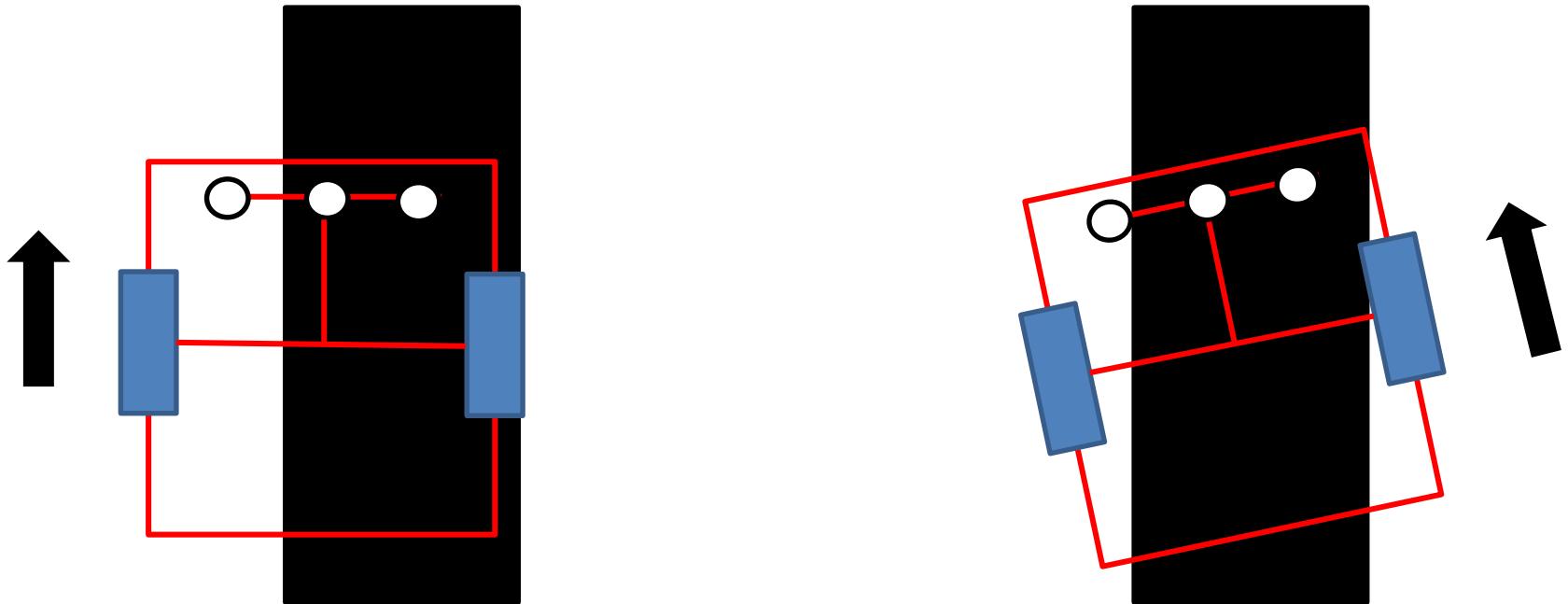


$$\textit{Steering} = K_{\textit{head}_P}(a) + K_{\textit{head}_d}(\dot{a})$$

$$\textit{Speed} = K_{\textit{speed}_P}(d) + K_{\textit{speed}_d}(\dot{d})$$

# Rule-based Control

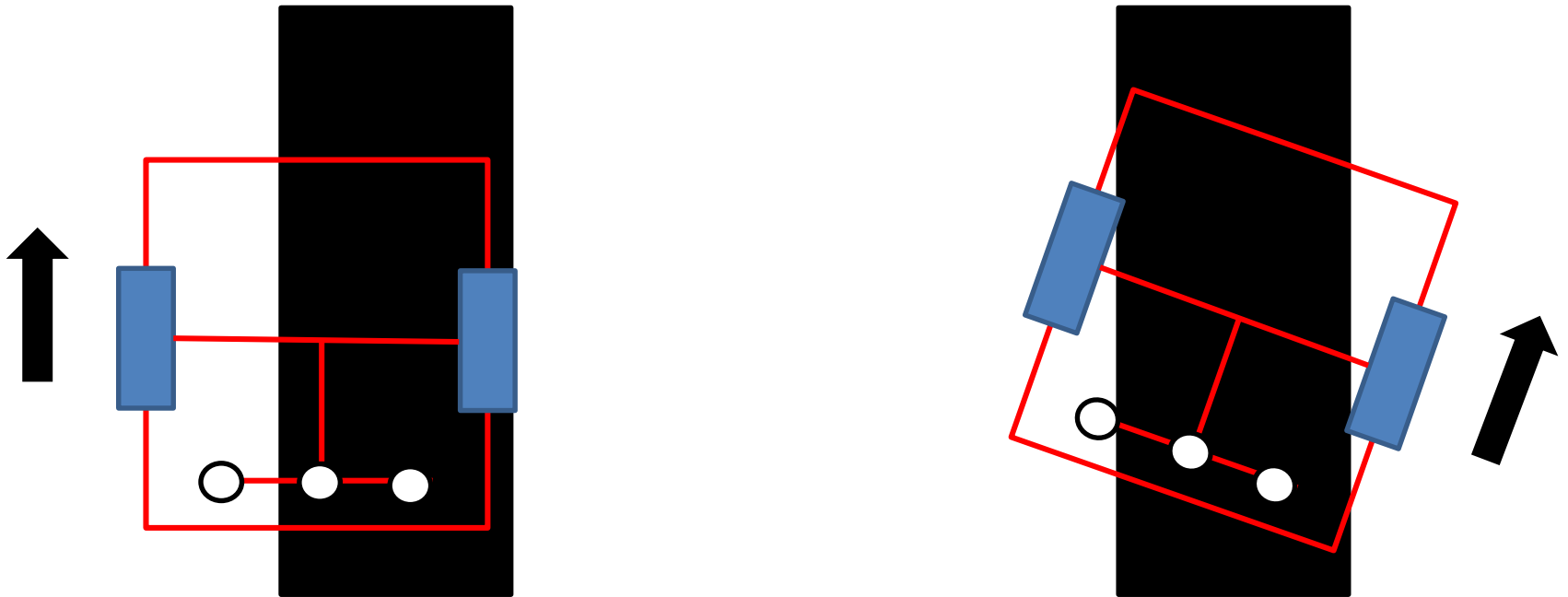
- For line tracking, sensor array should be installed in front of the robot center so that the actions of translation adjustment rule and rotation adjustment rule are not contradict and sensed by the same sensor.



- The robot should turn right for both translation and rotation adjustments to make the left sensor change the state.

# Rule-based Control

- If sensor array is installed behind the robot center the actions of translation adjustment rule and rotation adjustment rule are contradict as sensed by the sensor.

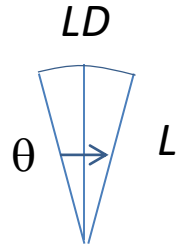


- The robot should turn right for translation adjustment but turn left for rotation adjustment.
- For translation adjustment, the left sensor doesn't change its state.

# Mobile Robot Localization

- Dead Reckoning System
  - Encoder
  - Compass
  - Line Tracking Sensor (Ir, LDR, etc.)
- Positioning System
  - Vision (Landmark, SLAM)
  - Laser, Sonar
  - GPS

# 4-Leg Locomotion Mechanism



– Leg Motion Distance ( $LD$  (m))

$$LD = \frac{2N\pi L}{R}$$

$N$  = Measured Pulse Number during Ground Contact

$L$  = Leg Length (m)

$R$  = Encoder Pulse per Revolution

– Robot Distance ( $RD$  (m))

$$RD = \frac{\sum_{i=1}^n LD_i}{n}$$

$LD_i$  = Leg no  $i$  Motion Distance during Ground Contact

$n$  = 1, 2, 3, or 4 depending on Number of Legs contacting Ground

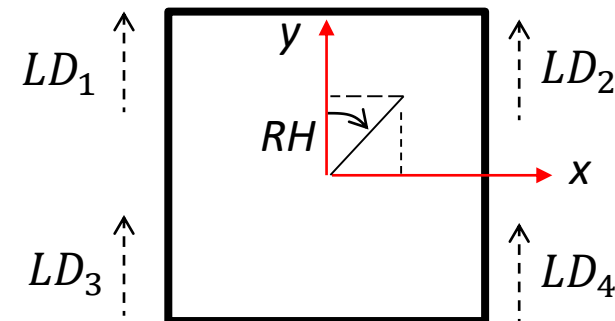
– Robot Heading ( $RH$  (degree) positive in clockwise direction))

$$RH = \frac{180(LD_1 - LD_2 + LD_3 - LD_4)}{n\pi D}$$

$D$  = Perpendicular Distance between  $LD$  vector and Robot Center

– Robot Coordinate ( $x$  (m),  $y$  (m))

$$x = \sum(RD \times \sin(\sum RH)) \quad y = \sum(RD \times \cos(\sum RH))$$



# Differential Wheeled Locomotion Mechanism

## – Wheel Distance ( $WD$ (m))

$$WD = \frac{N\pi D}{R}$$

$N$  = Measured Pulse Number

$D$  = Wheel Diameter (m)

$R$  = Encoder Pulse per Revolution

## – Robot Distance ( $RD$ (m))

$$RD = \frac{WD_L + WD_R}{2}$$

$WD_L$  = Left Wheel Distance

$WD_R$  = Right Wheel Distance

## – Robot Heading ( $RH$ (degree) positive in clockwise direction))

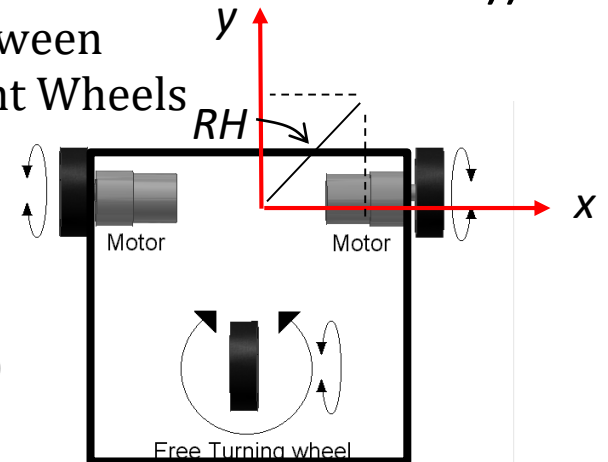
$$RH = \frac{180(WD_L - WD_R)}{\pi L}$$

$L$  = Distance between

Left and Right Wheels

## – Robot Coordinate ( $x$ (m), $y$ (m))

$$x = \sum(RD \times \sin(\sum RH)) \quad y = \sum(RD \times \cos(\sum RH))$$



# Omni Wheeled Locomotion Mechanism

– Wheel Distance ( $WD$  (m))

$$WD = \frac{N\pi D}{R}$$

$N$  = Measured Pulse Number

$D$  = Wheel Diameter (m)

$R$  = Encoder Pulse per Revolution

– Wheel Coordinate ( $x_i$  (m),  $y_i$  (m))

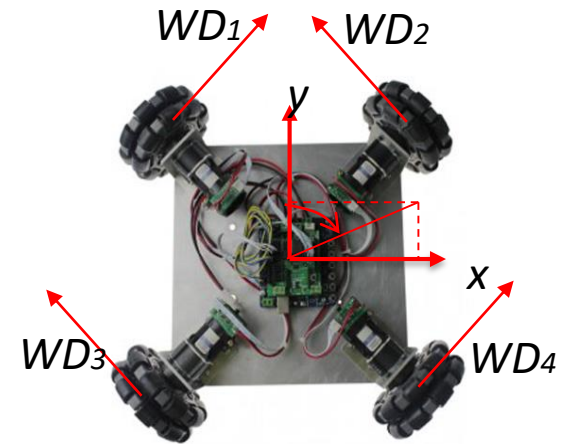
$$x_i = \frac{WD_i}{\sqrt{2}}$$

$$y_i = \frac{WD_i}{\sqrt{2}}$$

– Robot Coordinate ( $x$  (m),  $y$  (m))

$$x = \frac{x_1 - x_2 - x_3 + x_4}{4}$$

$$y = \frac{y_1 + y_2 + y_3 + y_4}{4}$$



– Robot Heading ( $RH$  (degree) positive in clockwise direction))

$$RH = \frac{180(WD_1 - WD_2 + WD_3 - WD_4)}{4\pi S}$$

$S$  = Perpendicular Distance between  
WD vector and Robot Center

# Mecanum Wheeled Locomotion Mechanism

- Wheel Distance ( $WD$  (m))

$$WD = \frac{N\pi D}{R}$$

$N$  = Measured Pulse Number

$D$  = Wheel Diameter (m)

$R$  = Encoder Pulse per Revolution

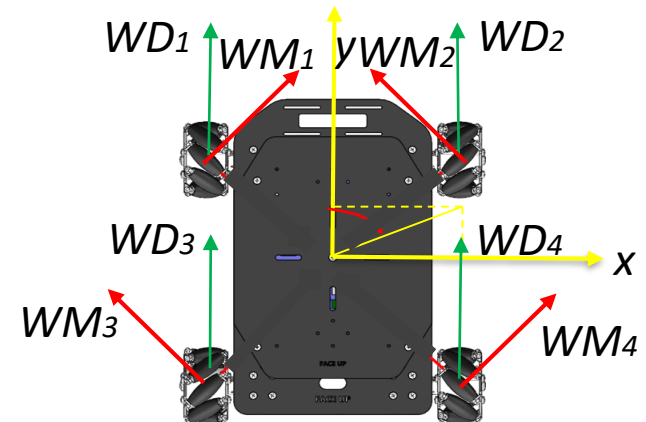
- Wheel Real Motion ( $WM$  (m))

$$WM_i = \frac{WD_i}{\sqrt{2}}$$

- Robot Coordinate ( $x$  (m),  $y$  (m))

$$x = \frac{WM_1 - WM_2 - WM_3 + WM_4}{4\sqrt{2}}$$

$$y = \frac{WM_1 + WM_2 + WM_3 + WM_4}{4\sqrt{2}}$$



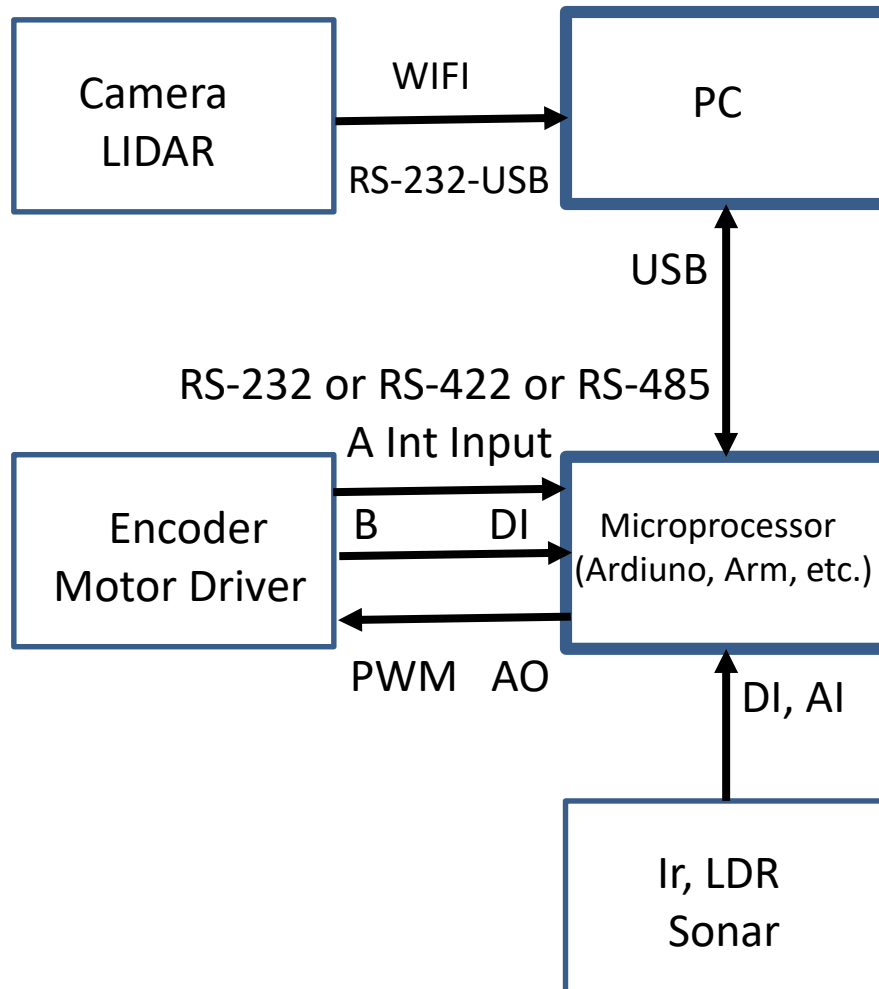
- Robot Heading ( $RH$  (degree) positive in clockwise direction))

$$RH = \frac{180(WM_1 - WM_2 + WM_3 - WM_4)}{4\pi C}$$

$C$  = Perpendicular Distance between  
WM vector and Robot Center



# Robot System Architecture



For GUI,  
Global Path Planning  
Local Path Planning  
Camera, LIDAR  
C#, C++ on Visual Studio or  
Python on Raspberry Pi

For Low Level Control  
Motor Driver  
Encoder  
Ir, LDR, Sonar  
C on Ardiuno or  
C on mbed.com -> Hardware ->  
Boards -> STMicroelectronics ->  
NUCLEO411RE (for Cortex M4)

Q & A